

User Manual 4.12 Numerical differentiation and integration

De Wiki

Aller à : [navigation](#), [rechercher](#)

[User Manual 4.12 Numerical differentiation and integration](#)

Introduction

Scope

This section details numerical differentiation and integration (not to be misunderstood with numerical integration of ODE). A focus is realised on:

- differentiation methods of real univariate functions: Ridders and finite difference.
- integration methods of real univariate functions : Trapezoidal and Simpson.

Javadoc

The numerical differentiator objects are available in the package `fr.cnes.sirius.patrius.math.analysis.differentiation`. The numerical integrator objects are available in the package `fr.cnes.sirius.patrius.math.analysis.integration`.

Library

Javadoc

Patrius [Package fr.cnes.sirius.patrius.math.analysis.differentiation](#)

Patrius [Package fr.cnes.sirius.patrius.math.analysis.integration](#)

Links

Links to the implemented integration methods :

<http://mathworld.wolfram.com/TrapezoidalRule.html>

<http://mathworld.wolfram.com/SimpsonsRule.html>

Useful Documents

None as of now.

Package Overview

The numerical differentiation conception is described hereafter :



Accuracy of integration method (all examples are based on sinus function):

Default setting	Value
Maximum absolute error	1.0e-15
Maximum relative error	1.0e-6

Maximum number of iterations 64

Minimum number of iterations 3

Note : the accuracy of the results and the computing time are directly dependent on the value of maximum relative error.

Features Description

Numerical differentiation

Finite difference

Finite difference is the discrete analog of the derivative. The user can choose the number of points to use and the step size (the gap between each point).

Ridders algorithm

The derivative of a function at a point x is computed using the Ridders method of polynomial extrapolation.

Numerical Integration

Trapezoidal method

The trapezoidal rule works by approximating the region under the graph of the function as a trapezoid and calculating its area.

```
UnivariateFunction f = new SinFunction();
UnivariateIntegrator integrator = new TrapezoidIntegrator();
double r = integrator.integrate(10000, f, 0, FastMath.PI);
```

Result : $r = 1.9999996078171345$ (exact result = 2)

And :

```
integrator = new TrapezoidIntegrator(1.e-12, 1.0e-15, 3, 64);
r = integrator.integrate(10000000, f, 0, FastMath.PI);
```

Result : $r = 1.9999999999904077$

But :

```
integrator = new TrapezoidIntegrator(1.e-13, 1.0e-15, 3, 64);
r = integrator.integrate(10000000, f, 0, FastMath.PI);
```

Result : $r =$ no result (infinite time !)

Simpson method

Simpson's rule is a Newton-Cotes formula for approximating the integral of a function using quadratic polynomials (i.e., parabolic arcs instead of the straight line segments used in the trapezoidal rule). In general, this method has faster convergence than the trapezoidal rule for functions which are twice continuously differentiable, though not in all specific cases.

```
UnivariateFunction f = new SinFunction();
UnivariateIntegrator integrator = new SimpsonIntegrator();
double r = integrator.integrate(10000, f, 0, FastMath.PI);
```

Result : r = 2.000000064530001 (exact result = 2)

Getting Started

[Modèle:SpecialInclusion prefix=\\$theme sub section="GettingStarted"/](#)

Contents

Interfaces

Interface	Summary	Javadoc
UnivariateFunctionDifferentiator	This interface represents a generic numerical differentiator.	...
UnivariateIntegrator	Interface for univariate integration algorithms.	...

Classes

Class	Summary	Javadoc
FiniteDifferencesDifferentiator	Apply the finite difference method to differentiate a function.	...
RiddersDifferentiator	Apply the Ridders algorithm to differentiate a function.	...
TrapezoidIntegrator	The class implements the Trapezoidal rule	...
SimpsonIntegrator	The class implements the Simpson rule	...

Récupérée de

«

http://patrius.cnes.fr/index.php?title=User_Manual_4.12_Numerical_differentiation_and_integration&oldid=3500 »

[Catégorie](#) :

- [User Manual 4.12 Mathematics](#)

Menu de navigation

Outils personnels

- [3.141.32.53](#)
- [Discussion avec cette adresse IP](#)

- [Créer un compte](#)
- [Se connecter](#)

Espaces de noms

- [Page](#)
- [Discussion](#)

Variantes

Affichages

- [Lire](#)
- [Voir le texte source](#)
- [Historique](#)
- [Exporter en PDF](#)

Plus

Rechercher

PATRIUS

- [Welcome](#)

Evolutions

- [Main differences between V4.15 and V4.14](#)
- [Main differences between V4.14 and V4.13](#)
- [Main differences between V4.13 and V4.12](#)
- [Main differences between V4.12 and V4.11](#)
- [Main differences between V4.11 and V4.10](#)
- [Main differences between V4.10 and V4.9](#)
- [Main differences between V4.9 and V4.8](#)
- [Main differences between V4.8 and V4.7](#)
- [Main differences between V4.7 and V4.6.1](#)
- [Main differences between V4.6.1 and V4.5.1](#)
- [Main differences between V4.5.1 and V4.4](#)
- [Main differences between V4.4 and V4.3](#)
- [Main differences between V4.3 and V4.2](#)

- [Main differences between V4.2 and V4.1.1](#)
- [Main differences between V4.1.1 and V4.1](#)
- [Main differences between V4.1 and V4.0](#)
- [Main differences between V4.0 and V3.4.1](#)

User Manual

- [User Manual 4.15](#)
- [User Manual 4.14](#)
- [User Manual 4.13](#)
- [User Manual 4.12](#)
- [User Manual 4.11](#)
- [User Manual 4.10](#)
- [User Manual 4.9](#)
- [User Manual 4.8](#)
- [User Manual 4.7](#)
- [User Manual 4.6.1](#)
- [User Manual 4.5.1](#)
- [User Manual 4.4](#)
- [User Manual 4.3](#)
- [User Manual 4.2](#)
- [User Manual 4.1](#)
- [User Manual 4.0](#)
- [User Manual 3.4.1](#)
- [User Manual 3.3](#)

Tutorials

- [Tutorials 4.15](#)
- [Tutorials 4.14](#)
- [Tutorials 4.13.5](#)
- [Tutorials 4.12.1](#)
- [Tutorials 4.8.1](#)
- [Tutorials 4.5.1](#)
- [Tutorials 4.4](#)
- [Tutorials 4.1](#)
- [Tutorials 4.0](#)

Links

- [CNES freeware server](#)

Navigation

- [Accueil](#)
- [Modifications récentes](#)
- [Page au hasard](#)

- [Aide](#)

Outils

- [Pages liées](#)
- [Suivi des pages liées](#)
- [Pages spéciales](#)
- [Adresse de cette version](#)
- [Information sur la page](#)
- [Citer cette page](#)

- Dernière modification de cette page le 19 décembre 2023 à 09:54.

- [Politique de confidentialité](#)
- [À propos de Wiki](#)
- [Avertissements](#)

- 